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LifeBrush: painting, simulating, and visualizing dense biomolecular environments

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ABSTRACT

LifeBrush is a Cyberworld for painting dynamic molecular illustrations in virtual reality (VR) that then come to life as interactive simulations. We designed our system for the biological mesoscale, a spatial scale where molecules inside cells interact to form larger structures and execute the functions of cellular life. We bring our immersive illustrations to life in VR using agent-based modelling and simulation. Our sketch-based brushes use discrete element texture synthesis to generate molecular-agents along the brush path derived from examples in a palette. In this article we add a new tool to sculpt the geometry of the environment and the molecules. We also introduce a new history based visualization that enables the user to interactively explore and distil, from the busy and chaotic mesoscale environment, the interactions between molecules that drive cellular processes. We demonstrate our system with a mitochondrion example.

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1 1. Introduction

Biological systems span from whole organisms, down to the
scale of viruses and individual molecules. At the mesoscale,
molecules interact to form more complicated structure and
function. The mesoscale mitochondrion is an internal compartment within the Eukaryotic cell that assembles adenosinetriphosphate (ATP) molecules, which are used by other cell
components to do work (Figure 1). The mitochondrion is a
dense and chaotic space, yet highly organised [1, 2]. A significant challenge for researchers has been communicating scinificant challenge at this level because visible light microscopes
do not reveal the functional components at this scale.

Scientific illustrators have confronted the challenges posed by the mesoscale. For instance, David Goodsell [2] is famous for his painstakingly detailed 2D watercolour paintings of mesoscale environments—his illustration of the mitochondrion is the inspiration for Figure 1. Meanwhile, animating mesoscale scenes was a laborious process for a team of 3D animators in Harvard's Biovisions project [3]. Imagine if we could paint these illustrations in 3D space and then have them come to life around us, to explore and manipulate.

The dense and chaotic mesoscale environments of the cell pose some significant challenges: (1) how to fill and simulate an environment with a large number of molecules and (2) how to visualise the chaotic interactions between molecules. Manual and random placement, together with agent-based simulation in a video game engine, was employed for Prokaryotic and Eukaryotic simulations [4, 5]. Klein et al. [6] use the power of the GPU to create large and densely packed mesoscale environments through parameterisation automatically.

Inspired by Goodsell's 2D illustration work, we created 31 LifeBrush [7] as a sketch-based Cyberworld to paint 3D 32 mesoscale illustrations in virtual reality (VR) that one can step 33 inside as they come to life (Figure 2). We propose novel visu-34 alisations to trace interactions between molecules as the simu-35 lation progresses through time. Our system couples interactive 36 sketch-based design with an agent-based model of molecular 37 interactions. 38

Agent-based modelling has been used to capture the swarm-

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ing behaviour of birds [8] and for modelling molecules in biological simulations [4, 5]. We use agent-based modelling to abstract the behaviour and interaction of molecules from the 3 underlying and expensive to compute quantum dynamics that 4 govern those interactions, which is essential for a real-time VR 5 environment. A molecular-agent in our system has a set of be-6 haviours and attributes that determines how it interacts with its 7 environment and other agents. We implemented an agent-based 8 framework that is capable of simulating and rendering 10,000 a agents at 90 frames-per-second in our mitochondrion example 10 (Section 3). 11

The user creates example arrangements and configurations of 12 agents in a palette (Figure 2). We paint molecules, derived from 13 the arrangements in the palette, along the brush-path, in space, 14 and on surfaces (Section 5). To generate the molecules, we use a 15 discrete element texture synthesis algorithm, that we previously 16 described in [9], that uses the palette as an example for synthe-17 sis. We propose a simple mapping to convert between our sys-18 tem's representation of an agent and the internal representation 19 of a so-called element within the texture synthesis framework 20 (Section 4). Switching back and forth between painting and 21 simulating enables iterative design possibilities (Figure 3). 22

In this extended article on *LifeBrush* [7] we added a sculpting tool, based on implicit surface modelling [10]. It enables the user to quickly sketch the geometry of the environment and the rough shape of proteins (Figures 13 and 11). The sculpting tool acts like virtual clay; the user either adds or removes the virtual clay with the brush point (Section 6).

In our original *LifeBrush* mitochondrion [7], it was difficult to observe and understand when and how molecular-agents interact. In this extended article, we propose a novel historical visualisation of events within the VR environment, where the user queries a set of agents and interactions to see a trace of the spatial history and sequence of events that led to the interactions (Section 7).

The complete source code and examples used in this article are available under an MIT open source license (https: //github.com/timdecode/LifeBrush). A video based on the figures in this article is available at https://youtu.be/ iOWU_LiCxKI.

41 2. Related work

42 2.1. Molecular Dynamics Construction and Visualization

There are many different techniques for producing 3D visual-43 izations of molecular and mesoscale structures [11, 12]. To 44 create molecular scenes, Packmol [13] and CellPack [14] ran-45 domly pack proteins and molecules onto surfaces and regions 46 inside of a virtual cell according to user-created recipe files. 47 Klein et al. [6] accelerate the packing process with GPUs. Koch 48 et al. [15] reduce visual clutter arising from ambient occlusion 49 artefacts in 3D multi-scale visualizations of molecular scenes, 50 while Kouřil et al. [16] address the problem of label placement 51 in dense 3D molecular scenes. CellView [17] is an interac-52 tive visualization tool for exploring multi-scale visualizations of 53 structures in the cell down to the molecular level. In LifeBrush 54



Fig. 1: The mitochondrion is an organelle in Eukaryotic cells. It generates most of the cell's adenosine triphosphate (ATP), a source of chemical energy. A proton gradient between the matrix space and cristae drives protons (in red) through ATP synthase (in green) enzymes in the inner mitochondrial membrane, causing the enzymes to spin. ATP synthase uses its kinetic energy to combine phosphate and adenosine diphosphate (ADP, in cyan) to produce ATP (green spheres). Hydrogen pumping proteins (in green) in the inner membrane move hydrogen from the matrix space to the cristae. To increase the number of ATP synthase enzymes the mitochondrion is packed with cristae, increasing its internal surface area and the rate of ATP synthesis. We sketched and simulated this mitochondrion, which contains 10,000 molecules, in VR using *LifeBrush*.

[7], we introduced interactive sketch-based design and simulation for molecular scenes, within VR. This article addresses limitations of that work, with new visualization and 3D sculpting tools.

2.2. Agent-based modeling and visualization

Agent-based approaches have been used to model biological 60 systems like swarming insects and birds [8], without relying on 61 purely mathematical models [18]. Agent-based systems have 62 also been used to model the Lactose operon inside E. coli bac-63 teria [19], for gene regulation [20] and immune system models 64 [21]. Along the lines of mathematical whole-cell models [22], 65 agent-based models have been applied to both Prokaryotic [4] 66 and Eukaryotic cells [5]. Meanwhile, multi-scale agent-based 67 models can simultaneously capture cells and groups of cells 68 at different scales [23, 24]. Automatic abstraction has been 69 used to reduce the computational complexity of such models 70 [25]. Pathline visualizations have been applied to swarm sys-71 tems [26, 27]. We follow a similar idea for path visualization, 72 but with the addition that the user can query events and agents 73 from a historical simulation timeline in VR. We have also added 74 a novel trace component to the visualization to trace dependen-75 cies between interactions. 76

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Fig. 2: Immersive design and simulation in VR. (a) Creating and configuring a new arrangement of molecular-agents (white outline) through a copy-paste operation from another set of molecular-agents (orange outline). (b) **Painting** the red agents from (a) into an agent-based simulation. (c) Stepping into an **immersive simulation**, the painted molecular-agents come to life. In the close-ups, molecules in the mitochondrion spin and pump red proton agents along the orange arrow.

2.3. Example-based texture synthesis, procedural modelling, and sketch-based synthesis

The goal of example-based texture synthesis algorithms is to 3 create a large non-repeating output that is similar to an input texture [28]. Pixel-based approaches synthesize 2D textures [29, 30, 31, 32, 33, 34]. Multi-scale 2D texture synthesis allows textures with very high [35] or infinite resolution [36]. Discrete element textures manipulate individual discrete elements instead of pixels. For example, texture bombing splatters small texture elements into a larger texture [37] and more recently this 10 has been optimized for on-the-fly generation on GPUs [38, 39]. 11 Hurtut et al. [40] and Landes et al. [41] consider the shape of 12 elements during synthesis. In this article, we use our interactive 13 discrete element texture synthesis algorithm, with support for 14 multiple textures in a palette, to generate agents [9]. This algo-15 rithm is related to the works of Ma et al. [42], Ijiri et al. [43] 16 and Roveri et al. [44]. We use a simple mapping from agents 17 to elements (Section 5), and as far as the authors are aware, 18 our original work [7] is the first to apply example-based dis-19 crete element texture synthesis to the problem of generating an 20 agent-based simulation. 21

Sketch-based interfaces apply the familiarity of real-world tools 22 like pencil and paper to interactive design problems, such 23 as 3D modelling [45]. Ecosystem simulation has been used 24 to synthesize and render large plant ecosystems [46]. Dis-25 crete element texture synthesis has been combined with sketch-26 based synthesis to allow the user to guide the synthesis pro-27 cess [43, 47, 48, 44, 9]. Ketabchi et al. [49] and Samavati 28 and Runions [50] apply interactive 3D content modelling to the 29 digital earth project. Sketch-based interfaces have also been 30 used to design and guide dynamic fluid simulations [51] and 31 for sketching crowds of agents [52]. A limitation of 2D sketch-32 based interfaces is how to embed a 2D curve from the computer 33 screen into a 3D space. The advent of consumer VR devices 34 solves some of the problems with 2D sketch-based synthesis, 35 by adding six degree-of-freedom input. For example, sketch-36 based interaction has been used in VR to paint curves in virtual 37

space [53]. We build on discrete element synthesis and sketchbased interaction for creating and configuring molecular-agents in a 3D VR simulation. 40



Fig. 3: An interactive exploration loop. We paint a simulation, press play and simulate. We pause, paint new agents and repeat. The example palette enables us to create new agent arrangements and configurations to paint into our simulations.

3. Large-scale agent-based simulation in Unreal Engine 4

An **agent** is defined by the set of *situations* that the agents can be in, its *actions*, its *internal data* and a *decision function* that determines what actions to take, given internal data and the current situation [54]. An agent interacts with other agents and its environment.

Our agent-based framework is built on the well known entitycomponent-system architecture [55], which we implemented within *LifeBrush*. In this architecture, we store the state of an

agent in components attached to the agent entity. Systems im plement agent behaviour by accessing and modifying the com ponents attached to an agent. We integrated our implementation
 with the Unreal Editor so that users can utilize Unreal's 3D wid gets, property editor interface, and serialization system [56].

For performance reasons, we chose to implement an entity-6 component-system (ECS) instead of using Unreal's actor-7 component model. The Unreal Engine is generalizable to a 8 wide variety of games. However, that generalizability meant a that we were not able to simulate more than a few hundred 10 molecular-agents in real-time. Consequently, we carefully op-11 timized our ECS implementation to store structures of the same 12 type in contiguous blocks of memory. Systems enumerate the 13 components of a given type, one after the other, enabling the 14 processor to keep data in its fast CPU-caches without access-15 ing its slow main memory. Efficient cache utilization and small 16 size structures are the primary reason that we can achieve higher 17 performance than the actor-component model that Unreal uses 18 natively. The Unity game engine has recently released a sim-19 ilar entity-component-system architecture to our implementa-20 tion and likewise, simulate a significant number of agents [57]. 21 To render so many agents, we apply GPU instancing, an 22 efficient technique that uses hardware features to reduce the 23 number of draw calls necessary to render many objects with 24 the same geometry and material properties. With so many 25 agents, running rigid body physics calculations on the CPU 26 is too expensive for a real-time simulation. Therefore, we in-27 tegrated Nvidia's Flex GPU particle-physics engine with our 28 entity-component-system [58, 59]. 29

30 3.1. Mitochondrial molecular-agents

Swarm agents implement rules that determine how they behave 31 when other agents fall within zones of interaction [8]. Follow-32 ing this model of swarm behaviour, we use interaction zone 33 rules to govern the behaviour of our molecular agents (see Fig-34 ure 4). We store the state of the agent behaviours in compo-35 nents, with the implementation of the rules defined in systems. 36 37 Each agent has a Flex particle that determines its physical interaction with other agents and the environment [58]. Except for 38 the molecular-agents on the mitochondrial surfaces, each agent 39 also has random walk behaviour to model Brownian motion. 40



Fig. 4: Molecular-agent behaviours. (a) The ATP synthase motor behaviour causes ATP synthase to spin when a hydrogen agent enters its interaction cone. (b) ADP is converted into ATP by a spinning ATP synthase. (c) Protons are pumped from within the interaction cone of a proton pump to the other side of the membrane. (d) The random walk behaviour causes an agent to randomly change direction at random time intervals, simulating Brownian motion.

4. Synthesizing molecular-agents

4.1. Discrete element texture synthesis

LifeBrush uses a discrete element texture synthesis algorithm that we developed previously (see [9]) to generate molecularagents. Agents are not elements in that system. A **discrete element** is a particle with a position, radius and an attribute vector to store user-defined attributes of the element. We use a map to convert back and forth between agents and elements (Figure 6).

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A discrete element texture has the property that the arrangement of elements is locally similar in a small window to other regions of the texture [28]. Our algorithm generates agents so that the windows around those elements are similar to windows in the example [9]. The algorithm requires a measure for how similar the attribute vectors of two elements are.

In *LifeBrush*, the attribute vector consists of two components, an *appearance* identifier and a *behaviour* identifier. The vector components are set during the mapping from agent to element. The *appearance* identifier is a unique integer for the combination of mesh and material properties of an agent. If two agents have the same mesh and material, they will have the same *appearance* identifier. The *behaviour* identifier is also an integer for the unique combination of components attached to an agent. If two agents have the same set of components, they will have the same *behaviour* identifier.

Let *a* and *b* be elements, with attribute vectors $[\alpha_a, \beta_a]$ and $[\alpha_b, \beta_b]$ respectively, where α_a is the appearance identifier for *a* and β_a is its behaviour identifier. The similarity measure between *a* and *b* is given by:

$$|a-b| = \omega_0(\alpha_a, \alpha_b) + \omega_1(\beta_a, \beta_b), \tag{1}$$

where ω_0 and ω_1 are customizable functions to compare two attributes. In our implementation, ω_0 and ω_1 are 0 when their parameters are the same and 1 when not. Our discrete element texture synthesis algorithm uses the element similarity measure to match elements that are the same (by appearance and behaviour) in the output and example [9]. With two attribute components, it is possible to synthesize two agents that look the same, but have different behaviours—we exploit this ability to paint new behaviour onto previously synthesized agents (Figure 10b).

4.2. Synthesizing agents

We paint with elements and we simulate with agents. When we switch between painting and simulating, we map elements to agents, and vice versa (Figure 5). An element in *LifeBrush* contains an additional data area. To map an agent to an element, we copy the agent (with its components) into the additional data area. Then, we set the appearance identifier and the behaviour identifier of the element's attribute vector. Now represented as elements, the element synthesis framework can use the neighbourhood similarity function (Equation 1) to generate new elements along the brush-path. Figure 6 contains an example mapping for our ATP Synthase agent.

Our element-synthesis framework (see Davison et al. [9]) is a separate plugin to *LifeBrush*. Its representation of an element is



Fig. 5: Our generative tools synthesize elements. When we simulate we map elements into agents. When we paint again, we map the agents back into elements. The additional data area of the element stores the agent state and configuration. The position maps to the element position. Each unique combination of agent appearance and behaviour gets a unique integer identifier. We store the appearance identifier and the behaviour identifier in the element attribute vector, which we use to compare the similarity of two elements during element synthesis.

compact, efficient and separate from an agent. In future work, we would like to include other element synthesis algorithms with their internal representations. Mapping allows us, and pos-

sibly other users of LifeBrush, to keep the representation of el-

ements separate from our representation of an agent.



Fig. 6: Mapping an ATP Synthase Agent to an Element. An ATP Synthase Agent has a component for ATP synthesis behaviour, a component for rigidbody interaction through the Nvidia Flex particle physics engine [58, 59], a mesh component with associated material, and a static position component to keep it anchored to the membrane surface. The unique combination of these component classes gets an identifier (for example, 42), which we map to the behaviour identifier of the Element. The mesh and material properties get another unique identifier (for example, 23) that maps to the appearance component of the Element. We copy components to the Element additional data area. Mapping the Element to an Agent copies the additional data area component back to the Agent.

5. Sketch-based simulation design in virtual reality

Inspired by physical pencil-and-paper interactions, sketchbased interfaces are used extensively for 3D modelling [45]. A challenge with 2D sketch-based interfaces is how to embed what is fundamentally a 2D curve created by a 2D input device 10 (mouse and keyboard or a digital pen) into a 3D environment. 11 Recent commodity hand-held VR controllers are 3D input de-12 vices, tracking position and orientation, that let the user sketch 13 curves directly in 3D space (see Google's Tilt Brush [53]). 14



Fig. 7: VR controller operation. (a) The user switches between different tools and settings by pointing their controller at a menu in VR. The size of the generation brush (b) and selection brush (c) is controlled by the analogue trigger button on the VR controller. (b) Clicking the top or bottom of the trackpad toggles different tool modes.

In LifeBrush, VR hand-held controllers are used for sketchbased interactions, navigation gestures and for interacting with a VR menu system (Figure 7). Through VR controllers the user interacts with the VR menu, to switch between different tools and to enter or leave the simulation mode.

We support room-scale VR navigation (Figure 2) and navigation gestures. Like an astronaut pulling his/her way through a space station, the grab gesture can be used to pull oneself through the world.

The **generative-brush** path *B* is composed of a set of spheres which have a position and a radius (bp_i, br_i) (Figure 9a). As the user sketches with the brush, the VR controller's analogue trigger button is used to set the radius of the brush spheres. The generative-brush synthesizes new elements within the set of brush spheres B. However, when it passes over previously synthesized elements, the position of those elements and the attribute vector are updated to reflect the example palette selection. Elements outside of the brush path are not affected. There are useful applications for this; for example, we use the generative brush to add ATP synthase behaviour to agents in a scene that did not have this behaviour before (Figure 10c).

With the filler tool, (Figure 9b) the user identifies a fill point where there are no elements, then we synthesize elements from that point until there is no more room to do so. The eraser (Figure 9c) removes elements within a certain distance along a brush path. The selection brush selects agents in a radius around the brush.

5.1. Assembling agents and desinging examples in the palette

The example palette is a space where the user designs arrangements of agents and configures their behaviour and other properties (Figure 2). To sketch agents into the simulation, we select agents from the palette, and an example-based synthesis algorithm uses the example to create agents along the brush path. See Davison et al. [9] for a more detailed description of this algorithm.

To create new example arrangements, or to modify existing arrangements, the user grabs agents with a VR controller to 51 move the agents around. We similarly duplicate agents. To 52 create a new agent, the user drags a mesh from the mesh library into the palette (Figure 8). The meshes are created with

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our sculpting tool (Section 6) or in an external 3D modelling 4 program like Maya [60]. We configure the newly created agent 2 with a property editor interface in VR. To add behaviours to 3 the agent, the user selects the behaviour from a behaviour com-4 ponent class library using a drop-down list. Some parameters, 5 such as numbers, can be difficult to modify with the VR inter-6 face, in which case the user can fall back to Unreal Engine's 2D 7 mouse and keyboard interface. To move an agent, the user grabs 8 it with a VR controller (by pulling the analogue trigger), to rea size they pull it apart with two hands. Another button allows 10 the user to duplicate an agent. 11



Fig. 8: Editing agent behaviour. In this screenshot, we just created an ATP synthase agent by dragging it from the mesh library to the right. We select an ATP Synthase behaviour from a library of behaviour component classes to give it that behaviour. We configure the properties of the agent, including the newly added ATP synthase component in a property editor.

¹² 5.2. An example LifeBrush session

In Figure 10 we describe an example iterative design session using *LifeBrush*. The session illustrates how a user can use *LifeBrush* to experiment with a simulation, using our sketchbased painting tools.

17 6. Implicit surface modeling in VR

The sculpting tool allows the user to create the 3D geometry 18 for molecular agents (Figure 11) and the simulation geometry 19 (Figure 13). As the user paints, the sculpting tool modifies a 3D 20 scalar field of density values, from which a surface reconstruc-21 tion algorithm (Lorensen and Cline [10]) converts the scalar 22 field into a 3D mesh. The user controls the size of the sculpting 23 brush with an analogue trigger button. Thus, it is possible to 24 create both fine and coarse meshes with the tool. 25

The scalar field is arbitrarily large. To efficiently construct a 26 3D mesh from the field in real-time we break the field down into 27 chunks (Figure 12). Then, for each recently modified chunk, we 28 efficiently construct a small mesh using marching cubes [10]. 29 The field is broken down into a sparse collection of chunks. If 30 there are no non-zero values in a chunk, it does not consume 31 memory. A chunk is a small grid of density values-for ex-32 ample, a 32^3 grid of scalar values. The chunks are so small, 33



(a) **Generative-Brush** New molecular-agents are synthesize along the brush path within the set of brush points *B*.



(b) **Filler Tool** We fill the empty region from the fill-point until there is no more space to add new molecular-agents.



(c) Eraser Removing elements along the brush stroke (orange dashed-line).

Fig. 9: Our sketch-based tools applied to a planar surface.

that we can construct the chunk meshes in real-time on a 5960x Intel processor running at 3.0 GHz. Before the user paints elements on the mesh, we merge the small chunk meshes into one mesh. We also have an option to trim the mesh to the simulation bounds (Figure 13).

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The sculpting tool supports two modes, addition or subtrac-39 tion. We increment the scalar value of cells overlapping the 40 brush point over time. Cells closer to the brush point increase 41 in value faster. Let s_i be the scalar value at position $p_i \in \mathbb{R}^3$ 42 and let p_t be the position of the sculpting tool point and r_t be 43 the current radius of the tool controlled by the trigger. At each 44 tick of the Unreal Engine [56] the updated value of the scalar 45 field at p_i is $s'_i = s_i + \delta t * (1 - |p_t - p_i|_2/r_t)$. If p_i is further 46 than r_t from p_t we do not update the value of the scalar field 47 s_i . This tool is good for creating smooth rounded objects. With 48 two controllers, it is possible to use this same technique to paint 49 with capsules instead of spheres. In this mode, instead of mea-50 suring the distance of a cell from the brush point, we measure 51 the distance of the cell from the line segment between the two 52 controllers and update the scalar field accordingly. In the future, 53



(a) Here we are sketching the initial state of a mitochondrion simulation. We painted the agents in this simulation from the example palette. At this point, the agents only have a random-walk behaviour and the simulation models an inactive mitochondrion.

(b) ATP synthase combines phosphate molecules with adenosine diphosphate (ADP) to create adenosine triphosphate molecules (ATP). We add this behaviour to the ATP synthase agents in the palette (using the editor in Figure 8). We brush over the old ATP synthase agents in the simulation to add the new ATP synthase behaviour from the example. We also paint ADP into the simulation. When we simulate, ADP binds to ATP synthase. However, we need a proton gradient to drive ATP synthase to produce ATP.



(c) Here we add proton agents (that represent a large number of protons) to the example palette and paint protons into the cristae (the central region). When there are more protons on the cristae side of the membrane relative to the other, this creates a charge gradient that drives protons through ATP synthase, causing it to spin and produce ATP.

Fig. 10: A design session where we used *LifeBrush* to paint and explore a mitochondrion simulation (video: https://youtu.be/HYLvN2qijeA).

field for each section using Crane et al.'s [63] fast algorithm.

ATP. In this step, we add a proton pump behaviour to some of the agents in the

example palette and paint that new behaviour onto the proton pumps in our

simulation. We simulate and observe the restoration of the proton gradient.

Eventually, ATP synthase starts spinning again and produces ATP.

we would like to add other tools for flattening the implicit surfaces and creating sharp geometries. We chose marching cubes [10] due to the simplicity of the implementation, an alternative and more sophisticated technique is dual-contouring [61].

We use the sculpting tool to create geometry in the environment, hence the user does not have to break immersion to use a third party modelling tool like Maya [60] or Blender [62]. It is also possible to use geometry imported from 3D modelling tools at the same time. In Figure 13 we use the sculpting tool to increase the internal surface area of our mitochondrion and hence the rate of ATP synthesis.

We integrated the sculpting tool with our discrete element texture synthesis system [9]. We identify the disconnected islands in the sculpted mesh and break the mesh into sections. In our discrete element framework, we calculate an orientation

The agent-building tool (Section 5.1) contains a library of 17 previously sculpted meshes and imported 3D meshes from ex-18 ternal 3D modelling programs. We generated some of the 19 agent-meshes from x-ray crystallography data available from 20 the protein data bank [64]. Creating meshes from the protein data bank takes time, in tools like Maya. Furthermore, the pro-22 tein databank is incomplete. Therefore, we found the sculpting 23 tool useful for quickly sketching protein meshes, which we may 24 later replace with true-to-life versions. Figure 14 contains some 25 example proteins that we sketched based on 2D illustrations by 26 David Goodsell [2]. 27



Fig. 11: Sketching the surface of an ATP synthase molecule using our sketchbased sculpting tool in VR. (left) New material is added along the brush path. (right) The complete ATP synthase mesh.



Fig. 12: (a) The scalar field is broken down into small chunks, typically with dimension 32^3 . When the brush modifies any value in a chunk, we mark the chunk as dirty. (b) We construct a new mesh for each dirty chunk using marchingcubes [10]. (c) Finally, we merge the meshes when the user stops using the sculpting tool.

7. Iteractive visualization with simulation timelines

In the original *LifeBrush* system it was challenging to observe interactions between molecular-agents in the dense and
busy mitochondrion environment [7]. Our proposed solution
to this problem is a history based visualization that highlights
molecular-agent interactions.

The timeline data structure is a historical record of interac-7 tion events and the state of the simulation at different points 8 in time. Whenever an agent triggers an interaction event, such 9 as an ATP-Synthase molecule creating an ATP molecule, we 10 record the event in the timeline. The event stores the time of 11 the interaction, the agent that triggered the interaction and the 12 other interacting agents. The timeline also records the position 13 of the agents every k seconds (the default value for k is 0.25s). 14 We have developed two interactive visualizations. Agent path-15 *lines* show the path agents have taken through the simulation. 16 An event trace visualizes a sequence of interactions between a 17 set of agents. 18

19 7.1. Agent pathlines

Pathlines in scientific visualization have been used to trace
the flow of virtual particles seeded from a starting position
through an unsteady vector field [65]. We visualize the paths
of molecular-agents as they course their way through the simulation (Figure 15). An underlying vector field does not drive the
agent trajectory. Instead, the trajectory of the agents is implicit
to the interactions between the agents.



Fig. 13: Sculpting the mitochondrial environment. (a) We use the capsule brush to sculpt new cristae regions between the two controllers. The scene also contains a mesh that we designed in Maya. (b) We trim the sculpted meshes to the simulation bounds and paint lipids and molecular-agents into the scene. The mitochondrion now has more internal surface area for ATP synthesis than in Figure 2c.



Fig. 14: Sculpted molecular agents. These are some molecules that we created with our sculpting tool. The purple proteins are widgets whose function is to fill the visual space of the mitochondrion (we only simulate their rigid body interaction with other molecules). The green proteins are a proton pump and an ATP synthase.

Agent pathlines twist and weave their way through the simulation space where other molecular-agents occlude them from view. To solve this problem, we hide occluding molecularagents that lie between the user's eyes and the pathlines. We do this efficiently in real-time by raycasting, from the eye position in the direction of each agent in the scene, against a boundingvolume-hierarchy of the pathline visualization [66]. We desaturate the appearance of the molecular-agents that were not queried by the user, to make the pathlines easier to see in VR.

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The user interacts with the pathline visualization by querying a set of molecular-agents with a selection brush. In Figure 15 we query the simulation after it has run for a few seconds. The pathline visualization reveals some interesting observations: 1) the central region was under pressure, that pushed the hydrogen agents (traces in red) to a region of lower pressure (the top in Figure 15b), and 2) there was a bias in the physics simulation that pushed agents from the left towards the top, instead of uniformly from either side of the central region. We are unsure where this bias comes from, but perhaps it is a property of the physics library we are using [58].

We found that the visualization tool had unexpected utility for debugging. For example, we did not notice when we were building our simulations, that some molecular-agents were tunnelling through the collision geometry, into regions they did



Fig. 15: Pathlines reveal the course taken by molecular agents in a simulation. (a) The initial state of a mitochondrial simulation, with hydrogen agents concentrated in the central region. After a few seconds we paused the simulation. (b) Querying the agents at the top (white dotted line), we see that the hydrogen agents moved from the central region to the top. There is a notable bias of left originating hydrogen agents. (c) With nowhere to go, the molecular-agents at the bottom followed a wandering path.



Fig. 16: Debugging with pathlines. We did not configure ADP to tunnel through the collision geometry like it is in this pathline visualization. We fixed the issue by modifying the collision parameters for the mesh.

not belong (Figure 16). We corrected the problem by modifying particle-surface collision properties. In another simulation,
we observed molecular-agents teleporting across the simulation
(Figure 17). The teleportation was due to a bug in the ATP synthase agent behaviour.

⁶ 7.2. Interaction event traces

When an event occurs, we place a 3D glyph (a coloured cube)
at the location of the event. The user interacts with the *event trace* visualization by selecting event glyphs with a VR controller.

For each selected event glyph, we trace forwards and backwards in the timeline from when the event occurred, looking for other events that reference the agents affected by the event. We do this recursively, up to a certain depth, and collate those events. Then we visualize the location of each collated event and produce a pathline visualization for the involved agents.

Fig. 17: Debugging with event traces. While visualizing proton pump behaviour, we noticed that hydrogen was teleporting across the simulation at random intervals. This visualization helped us notice and track down the bug in our code.

In Figure 18, we query an ATP synthesis event. The *event trace* visualization tells a story, where a hydrogen agent (red pathline) was driven through the ATP synthase molecule, giving it the energy to convert an ADP molecule into ATP, later that hydrogen agent was pumped back into the cristae (the central region of Figure 18a). Querying multiple events reveals the network of molecular-agent interactions in our mitochondrion (Figure 18c).

Event traces take a 4D dataset (spatiotemporal positions) and present it as a pathline. With the simulation paused, the user can take their time and explore a series of molecular interactions. As we mentioned, *event traces* tell the store of ATP synthesis and we think the visualization could have applications for explaining other molecular processes in mesoscale environments. 30

3D animations like Harvard's Biovisions project [3], use scripted and carefully animated video sequences to tell a story. Telling such a story with a simulation can be challenging, be-

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Fig. 18: *Event trace* visualizations reveal sequences of molecular-agent interactions. (a) The user selects event glyphs (the coloured cubes embedded in the simulation) with a brush tool, in the regions indicated by the white dashed lines. (b) Zooming into the central region, a molecular story unfolds. Hydrogen, pushed by a proton gradient, is driven through ATP synthase, giving it mechanical energy to convert ADP into ATP, which moves away. Meanwhile, the hydrogen agent wanders into a proton pump and is pushed back into the central region to maintain a proton gradient. (c) Our event trace visualization reveals the network of molecular-agent interactions over our mitochondrial membrane.

cause we may have to wait a long time for just the right sequence of interactions, that fit the story, to occur. Le Muzic
et al. [67] reduce the wait between events with a type of random interpolation. However, with pathlines, we can visualize
the time between events, while also visualizing past and subsequent interactions. Without editing the screenshots in an image
editor (other than to add annotations), we were also able to use
our visualization to explain mitochondrial function in several
2D figures in this article (such as Figure 1).

8. Discussion and future work

In our original LifeBrush paper, we painted and brought to life 11 a mesoscale illustration of the mitochondrion, in a VR Cy-12 berworld [7]. In this extended article, we describe additional 13 tools for sculpting environmental and molecular-agent geome-14 try with VR. Our example mitochondrion simulation is dense 15 and chaotic, replicating a real biomolecular system. Therefore 16 we have also extended our system with pathline and event trace 17 visualizations to understand that chaotic space. 18

Event trace visualizations are a useful tool for explaining and exploring agent interactions. We also found them useful for debugging. In the future, we would like to add a replay option. With a replay option, a *LifeBrush* simulation could be used in educational settings for students to interactively explore and experiment with mesoscale systems.

To generate and simulate the results in this article, we used 25 an Intel 5960x processor with eight cores running at 3.0 GHz 26 (the processor was released in 2014), 16 GB of RAM and an 27 Nvidia GTX 1080 GPU. We used an HTC Vive VR headset 28 and controllers. Our results run at 90 frames-per-second in VR 29 with about 10,000 agents. In the future, we could improve per-30 formance by multithreading our simulations and using level-of-31 detail techniques to reduce GPU overhead. 32

The target users for *LifeBrush*, include scientific illustrators, modellers, and computer scientists building mesoscale illustrations. We demonstrated an interactive sketch-based system; however, creating even simple molecular-agents requires writing C++ code. For users who can program, this is still a significant and time-consuming limitation. In the future, we plan to explore interactive and visual ways of defining molecular agent interactions to augment the programming interface. One possible solution is to provide the system with example agent interactions, such as with prototypical situation-action-pairs [68].

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Our sculpting tool is limited to capsular or spherical brushes. We want to add more brush types and functions. Another possibility is to add subdivision modelling tools.

In the future, we would also like to improve the accuracy of our mitochondrion illustration, especially with more function and behaviour. It would also be necessary to validate it against accepted models as well as biological in vivo experiments. However, even with our naive implementation, we think that it still has illustrative value. Future work will explore creating other mesoscale illustrations and simulations with our system.

In theory, we can extend our agent-to-element mapping to other agent-based systems and discrete element texture synthesis algorithms. For example, *LifeBrush* could be useful for painting crowd and ecosystem simulations. We would also like to incorporate Roveri et al.'s [44] algorithm for repetitive structure synthesis, among others.

Previous systems use recipe files to automatically pack molecules into mesoscale environments [13, 14, 6]. In contrast to these systems, we let the user interactively paint molecular agents into the mesoscale environment. We also demonstrated immediately bringing that environment to life within the same session. An exciting interaction is using our sketch-based tools to experiment with the simulation (Section 5.2) interactively.

Finally, an exciting possibility is collaborative editing and playback with LifeBrush in a multiplayer environment and across non-VR devices (like tablets and desktop computers). We imagine applications of our method for interactive illustration and teaching of mesoscale environments.

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